

# Further Musings on the Wang *et al.* MD5 Collision: Improvements and Corrections on the Work of Hawkes, Paddon, and Rose

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## Collision for MD5

$M_0$ : 02dd31d1c4eee6c5069a3d695cf9af9887b5ca2fab7e46123e580440897ffbb8  
0634qd5502b3f4098388e4835a417125e82551089fc9cdf7f2bd1dd95b3c3780

$M_1$ : d11d0b969c7b41dcf497d8e4d555655ac79a73350cfdebfo66f129308fb109d1  
797f2775eb5cd530baade8225c15c79ddcb74ed6dd3c55fd80a9bb1e3a7cc35

$M_0'$ : 02dd31d1c4eee6c5069a3d695cf9af9807b5ca2fab7e46123e580440897ffbb8  
0634qd5502b3f4098388e4835a41f125e82551089fc9cdf772bd1dd95b3c3780

$M_1$ : d11d0b969c7b41dcf497d8e4d555655a479a73350cfdebfo66f129308fb109d1  
797f2775eb5cd530baade8225c154c79ddcb74ed6dd3c55f580a9bb1e3a7cc35

$H$ : 9603161fa30f9dbf9f65ffbcf41fc7ef

**A collision occurs when two or more input messages produce the same message digest,  $H$ . In the case above,  $(M_0, M_1)$  and  $(M_0', M_1')$  yield the same value of  $H$ .**

## **Idea Behind My Paper:**

- The recent successful attack on the widely used hash function, the MD5 Message Digest Algorithm, was a breakthrough in cryptanalysis.
- The original paper, published in 2004 by Wang *et al.*, described this attack in an obscure and elliptical manner.
- Hawkes, Paddon, and Rose subsequently presented the attack in more detail, but even their paper contained numerous unproven statements and several significant errors.
- My paper will explicate their work, prove many of their assertions, and provide original corrections and illustrations to make the differential attack on MD5 more accessible to the mathematically literate reader.

## **Explication and Elaboration:**

- My paper provides the following explication and elaboration.
- First, it compares the unorthodox description of MD5 by Hawkes, Paddon, and Rose to the original description by Ron Rivest.
- Second, it supplies examples for the three conditions that they present for the  $T_t$  before they begin their description of the differential.
- Third, it expands on the description of the first block of the differential by explaining the conditions on the  $T_t$  in each step.
- Fourth, it presents an original step by step analysis of the description of the second block based only on the table that they provide.

## Assertions and Proofs:

- Hawkes, Paddon, and Rose provide assertions for all of bit conditions for the propagation of the differences through the  $f_t$  functions for the first block.
- My paper proves all of these assertions except for those mentioned in the sections labeled “Obtaining the Correct  $\Delta Q_t$ .” (since the discussion that they provide for these conditions was sufficient).
- My paper then provides a similar list of assertions for the propagation of the differences through the  $f_t$  functions for the second block based only on a few tables that they provide.
- My paper proves all of these assertions as well.

## Errors and Corrections:

- My paper corrects two significant errors in work of Hawkes, Paddon, and Rose.
- First, it demonstrates that the complexity of the attack is only about half as great as they believed, i.e., my paper proves the complexity to be  $2^{42}$  rather than  $2^{43}$ .
- Second, it shows that their *Case Two* does not succeed in fulfilling the conditions for the collision differential to hold.