

# Trusted Parties and Their Twins

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# Splittability! (The Disney Version)

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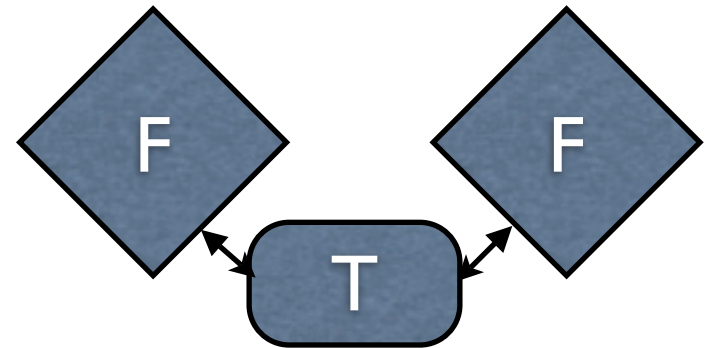
Haley Mills was indistinguishable from two coordinating copies of herself



≈



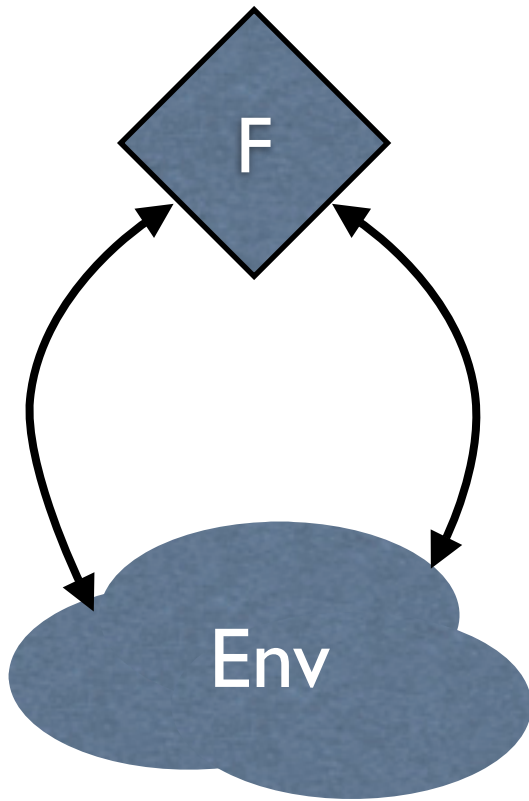
# Splittability! (The Disney Version)



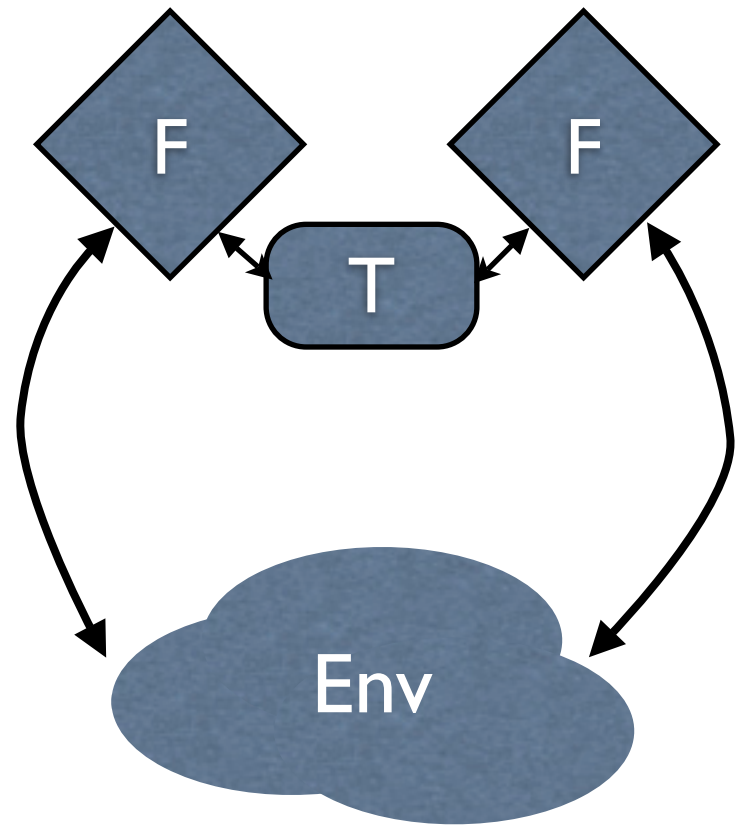
≈



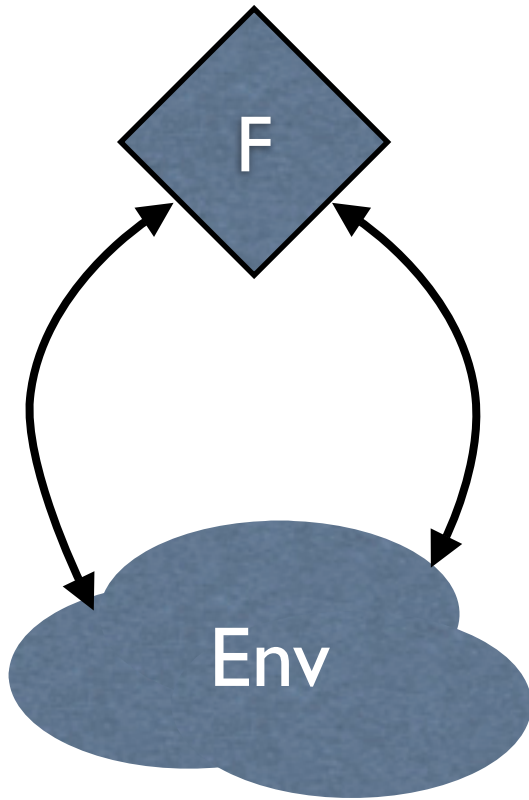
# Splittability!



≈

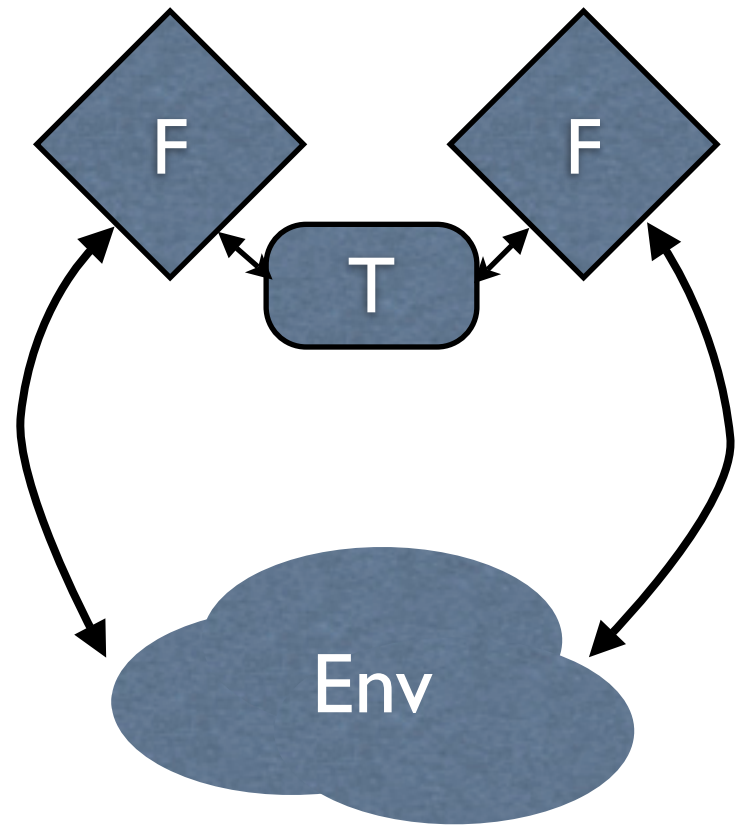


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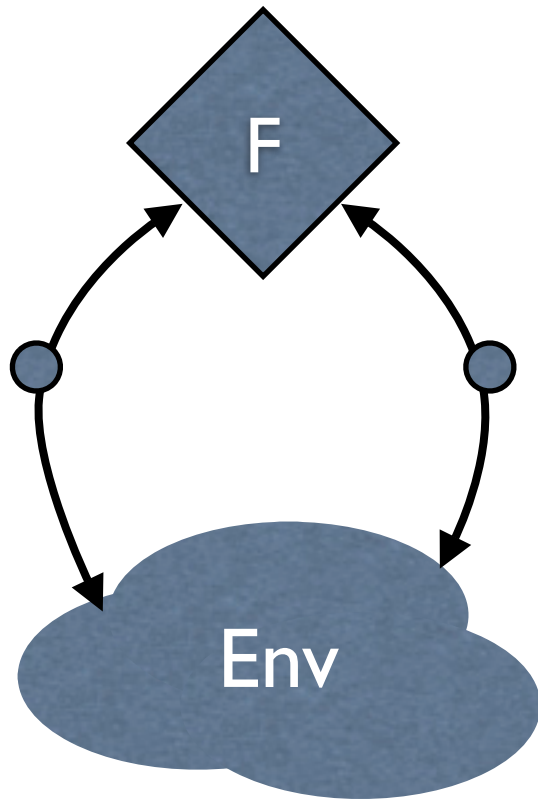
**F splittable**  
if  $\exists T$  s.t.  $F$  is  
indistinguishable  
from  $F \leftrightarrow T \leftrightarrow F$   
for all  
environments

$\approx$

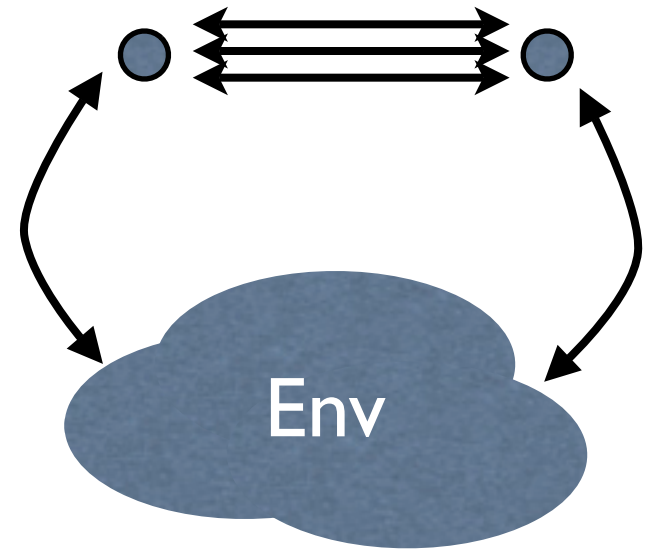




# Theorem: Splittable = Realizable



$\approx$

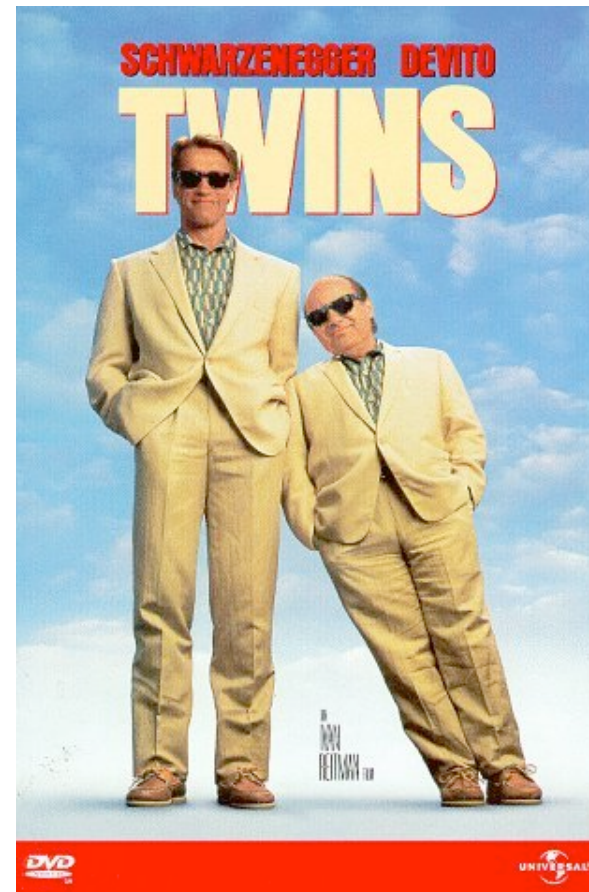




**When is there no  
protocol possible?**

# When is there no protocol possible?

If there's no way to keep the trusted party synchronized with its twin



# Using our characterization

- Easy to show impossibility of:
  - Commitment, simultaneous exchange, oblivious transfer, coin-flipping, ...
- Explicit and exact characterization for 2-party non-reactive functionalities
  - Subsumes impossibility of Canetti-Kushilevitz-Lindell'06
- Characterization holds also for m-party, reactive, randomized functionalities.
- Intriguing gaps/results for m-party ( $m > 2$ ) settings

# Generalization: Splittability Partial Order

- Extends to a partial order  $F < G$  (“F splits w.r.t. G”)
  - Gives results on realizability of F w.r.t G
  - Complete characterization when G is self-splittable ( $G < G$ ) !
- Other cute things...

# Hiding Functionalities

- Functionality version of one-way functions
  - e.g. oblivious transfer
- Can construct hardcore predicates for HFs
  - Then use to realize commitment, etc. (everything?)
  - Goldreich-Levin predicate for HFs!
  - Several open questions